

Determine if each function is continuous. If the function is not continuous, find the x-axis location of each discontinuity and classify each discontinuity as infinite or removable. Also find any horizontal asymptotes.

V.A. Hole

$$A) f(x) = \frac{3x^2 + 15x}{x+5} = \frac{3x(x+5)}{x+5}$$

P.O.D  
 $x+5=0$   
 $x=-5$   
 Hole  
 H.A.  
 None

$$B) f(x) = \frac{x^2 + 3x}{x+2} = \frac{x(x+3)}{x+2}$$

P.O.D  
 $x+2=0$   
 $x=-2$   
 V.A.  
 H.A.  
 None

$$C) f(x) = \frac{9x+6}{x^2-4} = \frac{3(3x+2)}{(x+2)(x-2)}$$

P.O.D  
 $x^2-4=0$   
 $(x-2)(x+2)=0$   
 $x=2, -2$   
 V.A. V.A.  
 H.A.  
 $y=0$

$$D) f(x) = \frac{9x+18}{x^2-4} = \frac{9(x+2)}{(x+2)(x-2)}$$

P.O.D  
 $x^2-4=0$   
 $(x+2)(x-2)=0$   
 $x=-2, x=2$   
 Hole V.A.  
 H.A.  
 $y=0$

$$E) f(x) = \frac{x-5}{x^2-4x-5} = \frac{x-5}{(x-5)(x+1)}$$

P.O.D  
 $x=5, x=-1$   
 Hole. V.A.  
 H.A.  
 $y=0$

If the degree on top  
Is greater by 1, then  
The graph will have a  
slant asymptote.

Find the slant asymptote

$$f(x) = \frac{3x^2 - 2x + 1}{x - 1}$$

$$\begin{array}{r|rrr} 1 & 3 & -2 & 1 \\ & & 3 & \\ \hline & 3 & 1 & \cancel{2} \end{array}$$

$$y = 3x + 1$$

$$f(x) = \frac{x^2 - 6x - 1}{x + 3}$$

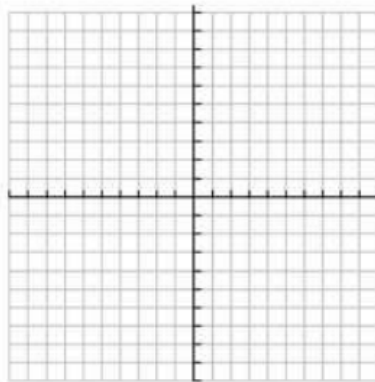
$$\begin{array}{r|rrr} -3 & 1 & -6 & -1 \\ & & -3 & 27 \\ \hline & 1 & -9 & \cancel{26} \end{array}$$

s.a.

$$y = x - 9$$

Graph the Function:

$$f(x) = \frac{x^2 - x - 6}{2x - 2}$$



Identify each point of discontinuity, holes, vertical asymptote, horizontal asymptote, zero(s), y-intercept, domain, and range.

Slant Asymptote

$$x+4=0$$

$$x=-4$$

$$\text{top} = 0$$

$$x-4=0$$

$$f(x) = \frac{x-4}{-4x-16} = \frac{x-4}{-4(x+4)}$$

$$f(x) = \frac{4}{x^2-3x} = \frac{4}{x(x-3)}$$

Zeros:  $x=4$

Zeros: None

y-intercepts:  $\frac{0-4}{-4(0)-16} = \frac{-4}{-16}$   
 $(0, \frac{1}{4})$

y-intercepts: None

#1 Points of Discontinuity:

$$x=-4$$

Points of Discontinuity:

$$x=0, x=3$$

$$x(x-3)=0$$

$$x=0 \quad x-3=0$$

$$x=3$$

Hole: None

Hole: None

Vertical Asymptote:

$$x=-4$$

Vertical Asymptote:

$$x=0 \quad x=3$$

Horizontal Asymptote:

$$y = -\frac{1}{4}$$

Horizontal Asymptote:

$$y=0$$

Domain:

$$(-\infty, -4) \cup (-4, \infty)$$

Domain:

$$(-\infty, 0) \cup (0, 3) \cup (3, \infty)$$

Slant Asymptote:

None

Slant Asymptote:

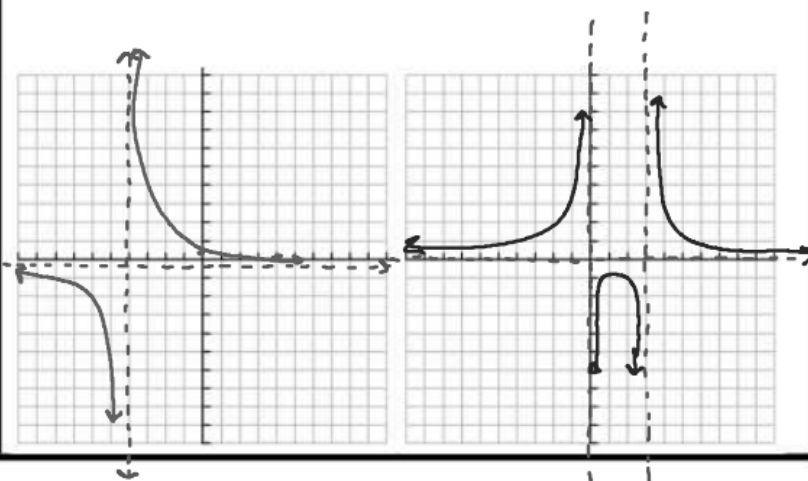
None

$$x=3.5$$

$$\frac{3.5-4}{-4(3.5)-16} = \frac{-0.5}{-14-16} = \frac{-0.5}{-30} = \frac{1}{60}$$

$$x=-5$$

$$\frac{-5-4}{-4(-5)-16} = \frac{-9}{20-16} = \frac{-9}{4} = -2.25$$



$$\frac{4}{x^2-3x}$$

$x=4$   
 $\frac{+}{+} \uparrow$   
 $x=2$   
 $\frac{+}{-} \downarrow$   
 $x=1$   
 $\frac{+}{+} \downarrow$   
 $x=-1$   
 $\frac{+}{+} \uparrow$

$$x(x-3)(x+3)$$

$$x=0 \quad x=3 \quad x=-3$$

$$\frac{0^3 - 9(0)}{3(0)^2 - 6(0) - 9} = \frac{0}{-9}$$

$$x = -.5$$

$$\frac{x^3 - 9x}{3x^2 - 6x - 9}$$

$$f(x) = \frac{x^3 - 9x}{3x^2 - 6x - 9} = \frac{x(x-3)(x+3)}{3(x-3)(x+1)}$$

Zeros:  $x=0$   
 ~~$x=3$~~   
 ~~$x=-3$~~   
 y-intercepts:  $(0,0)$

Points of Discontinuity:  
 $x=-1, x=3$

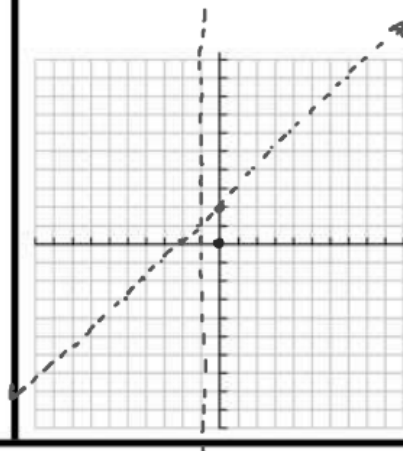
Hole:  
 $x=3$

Vertical Asymptote:  
 $x=-1$

Horizontal Asymptote:  
 None

Domain:  
 $(-\infty, -1) \cup (-1, 3) \cup (3, \infty)$

Slant Asymptote:  
 $y = x + 2$



$$f(x) = \frac{3x^2 - 12x}{x^2 - 2x - 3}$$

Zeros:

y-intercepts:

Points of Discontinuity:

Hole:

Vertical Asymptote:

Horizontal Asymptote:

Domain:

Slant Asymptote:

